

(i) Printed Pages : 3]

Roll No.

(ii) Questions : 8]

Sub. Code :

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Exam. Code :

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**B.A./B.Sc. (General) 5th Semester
Examination**

1127

**MATHEMATICS
(Modern Algebra)**

Paper : II

Time : 3 Hours]

[Max. Marks : 30

Note :- Attempt five questions in all, selecting at least two questions from each Section. All questions carry equal marks.

Section-A

1. (a) If $a, b \in G$ such that $ab = ba$ where G is a group, and $(o(a), o(b)) = 1$ then prove that :

$$o(ab) = o(a) o(b)$$

(b) Prove that the centre $Z(G)$ of a group G is a normal subgroup of G .

NA-82

(1)

Turn Over

2. (a) Prove that every quotient group of a cyclic group is cyclic.
- (b) Let H and K be two subgroups of a group G . Show that any coset relative to $H \cap K$ is the intersection of a coset relative to H with a coset relative to K .
3. (a) Let G and G' be two groups. If $f : G \rightarrow G'$ is a homomorphism, show that the kernel of f is a normal subgroup of G .
- (b) Prove that if for a group G , $f : G \rightarrow G$ is given by $f(x) = x^3$, $x \in G$ is an automorphism then G is abelian.
4. (a) If G be a non-abelian group such that $O(G) = p^3$, where p is a prime number, then prove that $O(Z) = p$, where Z is centre of G .
- (b) Prove that A_4 , alternating group of order 4, has no subgroup of order six.

Section-B

5. (a) Prove that a commutative ring R with identity $1 \neq 0$ is an integral domain iff the cancellation laws hold for multiplication.

- (b) If R is a ring in which $x^2 = x \forall x \in R$. Prove that R is a commutative ring of characteristics 2.
6. (a) Prove that union of two left (right) ideals of a ring is an ideal iff one is contained in the other.
- (b) Show that any ideal of Z is maximal iff it is generated by some prime element.
7. (a) Show that $M \neq \{0\}$ is a maximal ideal of a ring R iff for any ideal I of R , either $I \subseteq M$ or $I + M = R$.
- (b) Show that isomorphic images of an integral domain is an integral domain.
8. (a) If R is an integral domain, then prove that $R[x]$ is also integral domain.
- (b) For any ring R , show that :

$$R[x] \mid \langle x \rangle \cong R$$

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